New Features based on Multiple Word Graphs for Utterance Verification

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Abstract

The goal of Utterance Verification is to estimate a confidence measure which helps detecting words in the hypothesized sentence that are likely to have been misrecognized. Word graphs have been extensively employed for directly estimating the confidence measure and for extracting important predictor features. Moreover, the combination of the proposed features along with other kind of features provides improvements in the verification accuracy.

1. Introduction

Current speech recognition systems are not error-free and, in consequence, it is desirable for many applications to predict the reliability of each word of the hypothesized sentence. The goal of Utterance Verification (UV) is to detect words that are likely to have been misrecognized. This implies the estimation of a confidence measure for each hypothesized word to classify it as either correct or incorrect.

The usefulness of word graphs in UV for different purposes is well known. In [7] the proposed features based on word graphs are the most important predictors. In [4] the confidence measure is estimated on word graphs directly by the posterior probability of a hypothesized word given all the acoustic observations of the utterance. The word posterior probability based on word graphs is used in [8] along with a large set of other predictive features to improve speech recognition accuracy. In all the cases, the authors use a single word graph which is obtained through the recognition process. An overview of the posterior probabilities based on a single word graph is given in section 2.

In section 3 we propose three new features which are based on word posterior probabilities estimated on multiple word graphs. For the experimental study, in section 4.1, we describe our smoothed naive Bayes model which allows to profitably combine different kinds of features under a sound statistical framework [2]. In section 4.2 we describe a set of well-known features for using them along with the proposed features. In section 4.3 we describe the experimental task. In section 4.4 we evaluate the performance of the proposed features comparing them with the alternative predictor features.

2. Posterior probabilities on word graphs

A word graph $G$ is a directed, acyclic, weighted graph. The nodes corresponds to discrete points in time. The edges are triplets $[w, s, e]$, where $w$ is the hypothesized word from node $s$ to node $e$. The weights are scores associated to the word graph edges. Any path from the initial to the final node forms a hypothesis $h$.

Given the acoustic observations $\Theta^T$, the posterior probability for a specific word (edge) $[w, s, e]$ can be computed by summing up the posterior probabilities of all hypotheses of the word graph containing the edge $[w, s, e]$:

$$ P([w, s, e] | \Theta^T) = \frac{1}{P(\Theta^T)} \sum_{h \in G : w' = w, s' = s, e' = e} P(h, \Theta^T) $$

The probability of the sequence of acoustic observations $P(\Theta^T)$ can be computed by summing up the posterior probabilities of all word graph hypotheses:

$$ P(\Theta^T) = \sum_h P(h, \Theta^T) $$

These posterior probabilities can be efficiently computed based on the well-known forward-backward algorithm [4].

3. Features based on multiple word graphs

The posterior probabilities can be based on different kinds of knowledge depending on the weights associated to the word graph edges. In this work, we study three features:

- $\text{WgAC}$: the weights are acoustic scores.
- $\text{WgL}$: the weights are language model probabilities.
- $\text{WgTOT}$: the weights are the combination of acoustic and language model scores.
The algorithm proposed to compute each of these features is described in Figure 1. It is a general algorithm in the sense that it can be used to compute any feature based on multiple word graphs.

Let $W$ be the vocabulary of the task and let $G_t$ be a word graph which contains the most probable word-end partial hypotheses at time $t$ of the recognition process. Let WPos be an algorithm which, given a word graph $G_t$, computes the word posterior probabilities following the method described in section 2. We assume that the WPost algorithm returns a set $A$ composed by the edges of $G_t$ with the posterior probability estimation: $A = \{([w, s, e], p) : [w, s, e] \in G_t\}$.

The algorithm uses a matrix $C$ (of size $|W| \times T$) for storing the sum of the word posterior probabilities that any word $w \in W$ is obtained at any time $t \in \{1, \ldots, T\}$ of the recognition. This matrix is initialized to zero at the beginning of the algorithm. The computation of the feature is carried out in two stages:

**Stage 1**: It is performed during all the recognition process. For each recognition time $t$ do:

1. Compute the word posterior probabilities on the word graph $G_t$.
2. For each edge $[w, s, e] \in G_t$, the word posterior probability $p$ is accumulated to the posterior probabilities that the word $w$ have been obtained at each time $t'$ within the interval time $[s, e]$.

**Stage 2**: When the recognition process is finished, the feature is computed for each word of the most probable hypothesis $h_{best}$. First, the values stored in the matrix $C$ should be adequately normalized. Given a word $w \in W$ and a time $t \in \{1, \ldots, T\}$, the value $C(w, t)$ is restricted to the interval $[0, T - t + 1]$. The maximum value is due to this property [4]: the sum of the word posterior probabilities for a specific point in time must sum to one. Therefore, if a word $w$ is the only one that appears at time $t$ for all word graph $G_{t'} : t \leq t' \leq T$, the maximum value must be necessarily $T - t + 1$. The matrix values can be then properly normalized dividing each value $C(w, t)$ by the maximum value $T - t + 1$. Based on these normalized values, given a word $w$ and its starting and ending times $[s, e]$, two different variants of the feature are computed:

1. The average of the normalized values that the word $w$ is obtained in the interval time $[s, e]$.
2. The maximum normalized value that the word $w$ obtains in the interval time $[s, e]$.

The motivation of using multiple word graphs is based on two aspects. First, the usefulness of word graphs depends directly on the word graph density [9]. Thus, the use of multiple word graphs should provide a better representation of the most probable hypotheses. Another advantage is the capability of extracting the features at any time of the recognition process. This can be very useful for some applications such as continuous discourse to predict the reliability of partial hypotheses.

![Figure 1: Algorithm to compute one feature based on multiple word graphs.](image)

### 4. Experimental Study

#### 4.1. Naive Bayes model

We have recently proposed a smoothed naive Bayes classification model [2] to profitably combine different features. We denote the class variable by $c$; $c = 0$ for correct and $c = 1$ for incorrect. Given a hypothesized word $w$ and a $D$-dimensional vector of (discrete) features $x$, the class posteriors can be calculated via the Bayes’ rule as

$$P(c|x, w) = \frac{P(c|w) P(x|c, w)}{\sum_c P(c|w) P(x|c, w)} \quad (3)$$

We make the naive Bayes assumption that the features are mutually independent given a class-word pair. Unknown probabilities are estimated by direct relative frequencies. For robustness, this word-dependent (specific) model is smoothed using a word-independent (generalized) naive Bayes model [2].

UV is performed by classifying a word as incorrect if $P(c = 1 | x, w)$ is greater than a certain threshold $\tau$.

#### 4.2. Alternative predictor features

To compare the proposed features with alternative predictor features, a set of well-known features has been selected:

- **Acoustic stability (AS):** Number of times that a hypothesized word appears at the same position (as computed by Levenshtein alignment) in $K$ alternative outputs of the speech recognizer obtained using different values
of the Grammar Scale Factor (GSF), i.e. a weighting
between acoustic and language model scores [6].

**LMPr**: Language model probability.

**Hypothesis density (HD)**: The average number of the active
hypotheses within the word boundaries [7].

**PercPh**: The percentage of word phones that match the
phones obtained in a “phone-only” decoding.

**Duration** (Dur): The word duration in frames divided by its
number of phones.

**AcScore**: The acoustic log-score of the word divided by its
number of phones.

**Word Trellis Stability** (WTS): We have recently introduced
this feature [1]. Given a word \( w \) and its starting
and ending times \([s, e]\), two variants of the WTS are
computed as:

\[
WTS_{\text{avg}}(w) = \frac{1}{e-s+1} \sum_{t=s}^{e} C(w, t')
\]

\[
WTS_{\text{max}}(w) = \max_{s \leq t' \leq e} C(w, t')
\]

\[
C(w, t') = \frac{1}{T} \sum_{t'=1}^{T} \sum_{h \in \mathcal{H}_t(w, t')} (\alpha_{t'} - \alpha_t)
\]

where \( T \) is the number of frames of the given utter-
ance, \( \mathcal{H}_t \) is a set of word-boundary partial hypotheses
that are most probable at time \( t \) for a certain range
of GSF values \([\alpha_t, \alpha_{t'}]\). In addition, in each hypothesis of
\( \mathcal{H}_t(w, t') \) the word \( w \) must be active at time frame \( t' \).

### 4.3. Experimental setup

We carried out experiments using the FUB task, an Italian
speech corpus of phone calls to the front desk of a hotel, ac-
quired in the context of the EuTRANS project [5]. The FUB
corpus involves highly spontaneous speech data and contains
many non-speech artifacts. Basic statistics of the (disjoint)
training and test sets are summarized in table 1.

<table>
<thead>
<tr>
<th></th>
<th>training</th>
<th>test</th>
</tr>
</thead>
<tbody>
<tr>
<td>speakers</td>
<td>276</td>
<td>24</td>
</tr>
<tr>
<td>running words</td>
<td>5,211</td>
<td>5,381</td>
</tr>
<tr>
<td>vocabulary size</td>
<td>459</td>
<td>–</td>
</tr>
<tr>
<td>bigram perplexity</td>
<td>–</td>
<td>31</td>
</tr>
</tbody>
</table>

The training set was used to train Italian context-
dependent phone models. The acoustic models were left-to-
right continuous density HMMs, trained using Linear Dis-
criminant Analysis (LDA) and a Viterbi approximation [3].
Decision-tree clustered generalized triphones (CART with
1,500 tied states plus silence) were used as phone-units. A
smoothed trigram language model was estimated using the
transcriptions of the training utterances. The test-set Word
Error Rate was 27.5 %.

### 4.4. Experimental Results

We have used different metrics for the evaluation of the clas-
sification accuracy. In evaluating verification systems, two
measures are of interest: the True Rejection Rate (TRR), the
number of incorrect words that are classified as incorrect di-
vided by the number of incorrect words) and the False Re-
jection Rate (FRR, the number of correct words that are clas-
sified as incorrect divided by the number of correct words).
The trade-off between TRR and FRR values depends on a
decision threshold \( \tau \). A Receiver Operating Characteristic
(ROC) curve represents TRR against FRR for different val-
ues of \( \tau \). The area under a ROC curve divided by the area of a
worst-case diagonal ROC curve, provides an adequate over-
all estimation of the classification accuracy. We denote this
area ratio as AROC. Note that an AROC value of 2.0 would
indicate that all words can be correctly classified. Another
criterion is the Confidence Error Rate (CER) defined as the
number of classification errors divided by the total number
of recognized words. A baseline CER is obtained assuming
that all recognized words are classified as correct.

The training and the test data included \( N = 5,160 \) and
\( N = 5,131 \) samples \( \{[x_n, c_n, w_n]\}_{n=1}^{N} \) respectively, where
for each word \( w \) the class \( c \) and a vector of 20 features were
obtained: 12 features correspond to the two variants of the
three proposed features (WgAC,WgLM,WgTOT) computed
on a single and multiple word graphs. The other 8 features
are those described in section 4.2.

Table 2 shows the AROC, CER and the relative reduction in
baseline CER using the (single-feature) smoothed model.
As can be seen the WgLM feature gets the best AROC value
and outperforms significantly all the other features. Only
AS which has proved to be very useful [7, 6] achieves simi-
lar results. The WgTOT performance is slightly better than
WgAC. Although these two features are not better than AS
and WTS features, they outperform all the other features.
Thus, the use of the language model probabilities in the word
posterior estimations produce better results than the use of
acoustic scores. The large range of the acoustic scores is the
cause of this effect [4]. The variant used in the calculation of
the features seems to be negligible in the performance.

The naive Bayes model was employed to explore the per-
formance of feature combinations. All the possible com-
binations among the proposed features along with AS and
WTS features were tested. The other features were added
to the best combinations in order to achieve possible im-
provements. Table 3 shows the AROC, CER and the rela-
tive reduction in baseline CER for the best feature combi-
nations. The combination of the two best single features:
WgLM+AS produces a significant improvement over the
single feature performance. The incremental addition of
new features to this combination produces further improve-
ments, finally achieving a relative reduction in baseline CER
of 37.6%. Figure 2 shows the ROC curves for the best single
feature and the best feature combination. It shows the gain
by exploiting the (naive Bayes) combination of features.
Table 2: AROC, CER and relative reduction in baseline CER for each individual feature.

<table>
<thead>
<tr>
<th>Feature</th>
<th>AROC</th>
<th>CER(%)</th>
<th>rel. red. (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>WgLMavg</td>
<td>1.73</td>
<td>16.4</td>
<td>21.9</td>
</tr>
<tr>
<td>WgLMmax</td>
<td>1.72</td>
<td>16.4</td>
<td>21.9</td>
</tr>
<tr>
<td>AS</td>
<td>1.70</td>
<td>16.3</td>
<td>22.4</td>
</tr>
<tr>
<td>WTSmax</td>
<td>1.68</td>
<td>17.9</td>
<td>14.8</td>
</tr>
<tr>
<td>WTSavg</td>
<td>1.66</td>
<td>18.2</td>
<td>13.3</td>
</tr>
<tr>
<td>WgTOTmax</td>
<td>1.65</td>
<td>18.0</td>
<td>14.3</td>
</tr>
<tr>
<td>WgACmax</td>
<td>1.63</td>
<td>18.7</td>
<td>11.0</td>
</tr>
<tr>
<td>WgTOTavg</td>
<td>1.61</td>
<td>18.4</td>
<td>12.4</td>
</tr>
<tr>
<td>WgACavg</td>
<td>1.61</td>
<td>19.0</td>
<td>9.5</td>
</tr>
<tr>
<td>LMPr</td>
<td>1.59</td>
<td>18.8</td>
<td>10.5</td>
</tr>
<tr>
<td>HD</td>
<td>1.59</td>
<td>18.9</td>
<td>10.0</td>
</tr>
<tr>
<td>PercPh</td>
<td>1.51</td>
<td>19.4</td>
<td>7.6</td>
</tr>
<tr>
<td>Dur</td>
<td>1.48</td>
<td>19.3</td>
<td>8.1</td>
</tr>
<tr>
<td>AcScore</td>
<td>1.48</td>
<td>19.6</td>
<td>6.7</td>
</tr>
<tr>
<td>Baseline</td>
<td>-</td>
<td>21.0</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 3: AROC, CER and relative reduction in baseline CER for the best feature combinations.

<table>
<thead>
<tr>
<th>Features</th>
<th>AROC</th>
<th>CER(%)</th>
<th>rel. red. (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AcScore+WgTOTmax+</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>WTSmax+Dur+AS+WgLMavg</td>
<td>1.81</td>
<td>13.1</td>
<td>37.6</td>
</tr>
<tr>
<td>WTSmax+Dur+AS+WgLMavg</td>
<td>1.81</td>
<td>13.6</td>
<td>35.2</td>
</tr>
<tr>
<td>Dur+AS+WgLMmax</td>
<td>1.79</td>
<td>14.4</td>
<td>31.4</td>
</tr>
<tr>
<td>AS+WgLMnorm</td>
<td>1.78</td>
<td>14.5</td>
<td>31.0</td>
</tr>
<tr>
<td>WgLMavg</td>
<td>1.73</td>
<td>16.4</td>
<td>21.9</td>
</tr>
<tr>
<td>Baseline</td>
<td>-</td>
<td>21.0</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 4 shows the AROC and CER of using a single or multiple word graphs in the computation of the features. The use of multiple word graphs produces better AROC values for all the features. The improvements are most significant for the WgTOT and WgAC features. This fact suggests that the use of multiple word graphs helps reduce the negative impact of the large range of acoustic scores. Nevertheless, although AROC values indicate that the use of multiple word graphs achieves better overall verification performance, the differences between CER values are not significant.

5. Conclusions

We have proposed three new features for utterance verification. These features are based on word posterior probabilities estimated on single word graphs and other well-known predictor features. The single feature performance is improved through the (naive Bayes) combination of the proposed features along with other kind of features.

6. Acknowledgements

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7. References